

# Rate-Distortion Optimized Rate Control for Depth Map-Based 3-D Video Coding

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**Abstract**—In this paper, a novel rate control scheme with optimized bits allocation for the 3-D video coding is proposed. First, we investigate the R-D characteristics of the texture and depth map of the coded view, as well as the quality dependency between the virtual view and the coded view. Second, an optimal bit allocation scheme is developed to allocate target bits for both the texture and depth maps of different views. Meanwhile, a simplified model parameter estimation scheme is adopted to speed up the coding process. Finally, the experimental results on various 3-D video sequences demonstrate that the proposed algorithm achieves excellent R-D efficiency and bit rate accuracy compared to benchmark algorithms.

**Index Terms**—3-D video coding, depth map, rate control, view synthesis.

## I. INTRODUCTION

THREE-DIMENSIONAL VIDEO (3DV) has gained increasing interests recently. The typical 3DV is stereoscopic video which provides each eye with one video separately at the same time. The small differences between these two videos cause the illusion of depth perception for human. In addition to the stereoscopic 3D video, the emerging autostereoscopic display [1]–[4] which emits a number of views enable autostereoscopic 3D video. Comparing with stereoscopic viewing, it involves a more general case of  $n$ -view multiview video. In this scenario, the viewpoint can be interactively changed by selecting different stereo pairs of views from  $n$ -view.

Delivering or storing  $n$ -view video requires tremendous bits that beyonds current transmission or storage capacity. Multiview Video Coding (MVC) [5] is developed to encode the multiview videos, where both the temporal redundancy within each view and inter-view redundancy among the neighbouring views are exploited [6]. Although the MVC encoder performs excellent coding efficiency, it is still not efficient enough to

Manuscript received March 1, 2012; revised September 3, 2012; accepted September 4, 2012. Date of publication September 20, 2012; date of current version January 10, 2013. This work was supported by the Hong Kong Research Grants Council General Research Fund, under Project 9041495 (CityU 115109) and the National Nature Science Foundation of China under Grant 61102088. The associate editor coordinating the review of this manuscript and approving it for publication was Dr. James E. Fowler.

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Digital Object Identifier 10.1109/TIP.2012.2219549

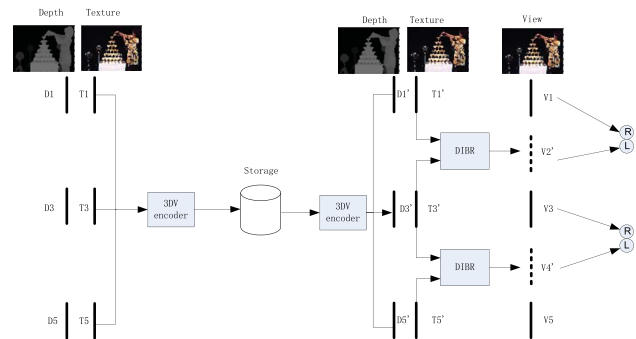


Fig. 1. Overview of 3-D video coding system.  $m$  views are encoded at the sender side and decoded at the receiver side. The virtual views are synthesized with DIBR by referencing the decoded views at the receiver side.

store or to transmit large numbers of views. Multiview plus depth format (MVD) [7], [8] presents a promising solution for the efficient delivery of 3DV. As shown in Fig. 1, only a subset  $m$  of  $n$  views are coded and transmitted, along with additional supplementary information such as per-pixel depth map which provides scene geometry information. At receiver side, these  $m$  coded views provide references for generating the rest views, which are synthesized as the virtual views via Depth-Image-based-Rendition (DIBR) [9], [10]. MVD reduces the number of the views to be transmitted but it can still reconstruct all the required views at the receiver side.

Rate Control (RC) is employed in video coding to regulate the bit rate meanwhile guarantee good video quality. As for 3DV, it becomes more complicated because multiple views are involved in coding and within each view there are two kinds of video sequences (*i.e.* texture and depth map). One of challenge problems is the bit allocation between the texture and depth map. Since the quality of virtual view is affected by the quality of both the texture and depth map, the bits should be allocated to balance their quality. In [11], bits are allocated to minimize the total distortion of the texture and depth map. However since the depth map is not presented for viewing, the minimum total distortion does not guarantee the optimal quality in the virtual views. In [12] the optimal bit allocation between the texture map and depth map is exhaustively searched by a hierarchical search method. In [13], the distortion of the virtual view is modeled and the optimal bit allocation between the texture and depth map is searched based on this distortion model. In [14], a similar distortion model is derived for virtual view and to achieve optimal virtual view quality, bits are allocated between the texture and depth map based on the derived distortion model. In [15], a joint

RC scheme is proposed where inter-view bit allocation are performed according to the sequence complexity of each view, while the bits are allocated at fixed ratio between texture and depth map within each view. However in these algorithms, inter-view bit allocation is rarely considered or only simply allocated according to the sequence complexity. In 3DV, more general case involves  $m$  views coding, thus bits allocation among different views is highly desired.

In this paper, the RC algorithm is proposed aiming at improving the overall quality in 3DV, where both the qualities of the coded views and the virtual views are considered. This is more reasonable, since both the virtual view and the coded view would be presented for viewing at the receiver side. On the other hand, the virtual view is synthesized by referencing nearby coded views, thus its quality depends on the coded references' quality. As shown in Fig. 1, different coded views are referenced by different number of virtual views. Intuitively, the coded view with more dependants should have better quality, as it would benefit more virtual views. In order to achieve the optimal R-D performance in 3DV, we first investigate the R-D characteristics of the texture and depth map. Then the quality dependency between the virtual view and the coded view is studied in the texture and depth map respectively. Based on the R-D characteristics of both the coded view and the virtual view, a bit allocation scheme is proposed for both the texture and depth map of all coded views. In this paper, a simple case of multiview 3DV is discussed, where only three views are coded and two views are synthesized, but the bit allocation scheme and the conclusions derived in this paper can be easily extend to  $n$  views cases.

The rest of this paper is organized as follows. In Section II, the R-D characteristics of both the coded view and the virtual view are investigated. In Section III, a RC scheme is proposed with optimal bit allocation. In Section IV, the experimental results are given to demonstrate the efficiency of the proposed RC algorithm. Finally, Section V concludes this paper.

## II. RATE AND QUALITY ANALYSIS IN 3-DV

### A. R-D Model for Coded Views

The tradeoff between the output bit rate ( $R$ ) and the quality ( $D$ ) of compressed video is determined by quantization step size ( $Q_s$ ), which is indexed by quantization parameter ( $Q$ ). The  $R$ - $Q_s$  and  $D$ - $Q_s$  model have been studied extensively for previous video coding standards such as MPEG-2 and H.264/AVC.

For the  $R$ - $Q_s$  model, the classic quadratic model is developed in [16], [17] and a linear model is widely studied and applied for its simple form [18]–[20]. In 3DV, the R-D characteristics is different from that in previous coding standards. First, the depth map is a grey image, which has no chrominance (UV) components for YUV color space. Second, the inter-view prediction is employed to reduce the redundancy among the different views. We employ the power  $R$ - $Q_s$  model [21], [22] for the depth and texture map as

$$R = \rho Q_s^\tau + c \quad (1)$$

where model parameter  $\rho$  and  $\tau$  depend on the video content and the sequence types (*i.e.* texture or depth map);  $c$  represents

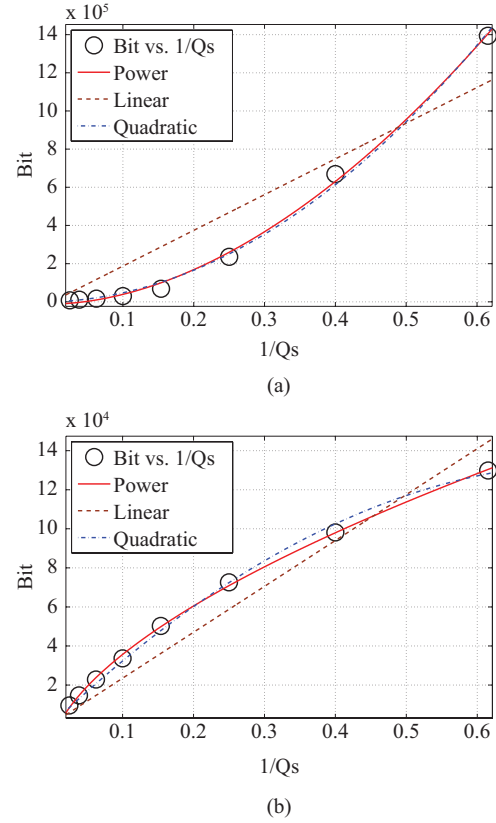


Fig. 2. R-Q relationship in the texture and depth map for the sequence *Kendo*. (a) Texture map. (b) Depth map.

the bit to code the header information. At high bit rate, header bits usually take a small part of the total output bits, therefore we simplify (1) by ignoring the header bits as

$$R \approx \rho Q_s^\tau \quad (2)$$

In Fig. 2, video sequence *Kendo* is coded with  $Q$  from 8 to 36. We can see that both the power model and the quadratic model fit the actual data well. For its simple form, the power model is adopted in our work. In Fig. 2, the texture and depth map exhibit different R-D characteristics. For example, parameter  $\tau$  is quite different in the texture map and depth map.

In H.264/AVC and its MVC extension,  $Q_s$  and  $Q$  have non-linear relationship, *i.e.*,  $Q_s$  double in size for every increment of 6 in  $Q$  [23]. This relationship can be approximated as

$$Q_s \approx e^{c_1 Q + c_2} \quad (3)$$

where  $c_1$  and  $c_2$  are constants that  $c_1 = \frac{1}{6} \ln 2$  and  $c_2 = -\frac{2}{3} \ln 2$ . Therefore  $R$ - $Q$  relationship can be derived by substituting (3) into (2) as

$$R = \rho \cdot e^{\tau(c_1 Q + c_2)} \quad (4)$$

As for the  $D$ - $Q$  model, we investigate the relationship between  $Q$  and the quality of texture map. Since the depth map will not be presented for viewing,  $Q$  of depth map will have no direct effect on view quality, but it will have indirect influence on the quality of virtual view. Such influence will

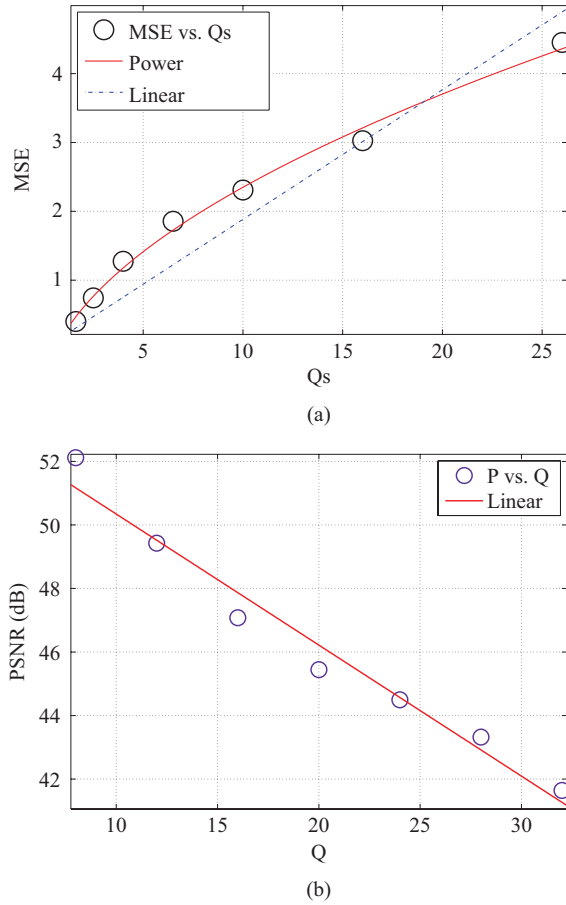


Fig. 3.  $D$ - $Q$  relationship in the texture map for the sequence *Balloons*. (a)  $MSE$ - $Q_s$  relationship. (b)  $PSNR$ - $Q$  relationship.

be discussed in Section II-B. For the texture map, the  $D$ - $Q$  model is adopted as

$$MSE = \chi Q_s^\varphi \quad (5)$$

where  $MSE$  is mean square error indicating the quality of reconstructed pictures;  $\chi$  and  $\varphi$  are model parameters related to the video content. The  $MSE$ - $Q_s$  relationship is illustrated in Fig. 3(a), where  $Q$  varies from 6 to 32. We can see that the actual relationship can be precisely depicted by (5).  $MSE$  and peak signal noise ratio (PSNR) have following relationship

$$P = 10 \log_{10} \left( \frac{255^2}{MSE} \right) \quad (6)$$

where  $P$  refers to PSNR. By substituting (3) and (6), we obtain the  $P$ - $Q$  relation as

$$P = \alpha Q + \eta \quad (7)$$

where  $\alpha = -\frac{10}{\ln 10} c_1 \varphi$  and  $\eta = \frac{10}{\ln 10} (\ln \frac{255^2}{\chi} - \varphi c_2)$ . The  $P$ - $Q$  relationship in (7) is illustrated in Fig. 3(b). As we can see, the PSNR decreases almost linearly with increase of  $Q$  value.

### B. Quality Analysis for Virtual Views

At the receiver side, the virtual views can be synthesized from nearby coded views with DIBR as shown in Fig. 1. In this paper, we investigate in the multiview video captured

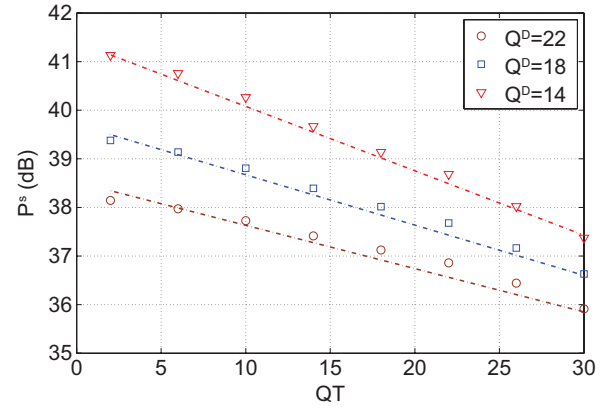


Fig. 4. Linear relationship between the quality of virtual view and  $Q^T$  on the sequence *Champagne\_tower*. View 37 is coded while view 38 is synthesized with DIBR.  $Q^T$  is changed from 2 to 30 when  $Q^D$  is fixed at 14, 18, and 22, respectively.

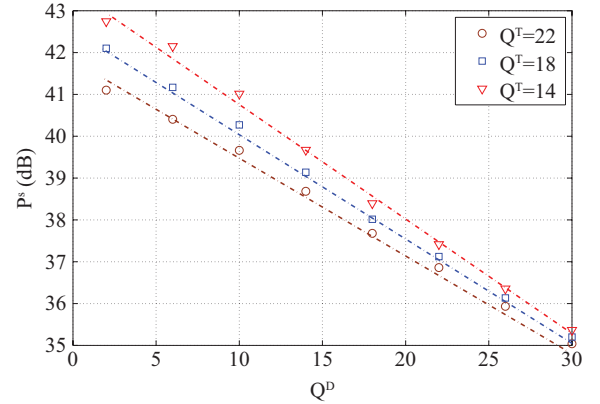


Fig. 5. Linear relationship between the quality of virtual view and  $Q^D$  on the sequence *Champagne\_tower*. View 37 is coded while view 38 is synthesized with DIBR.  $Q^D$  is changed from 2 to 30 when  $Q^T$  is fixed at 14, 18, and 22, respectively.

by parallel camera array with small intervals. When DIBR is applied at receiver side, distortion will be introduced due to the compression error in the texture and depth map. In [24], analysis on the effect of geometry distortions caused by depth coding artifacts is presented. In [25], the bound of synthesis error is derived for various configurations such as depth errors. Even without compression, the distortion would be introduced by the DIBR tools. Various DIBR algorithms have been proposed to reduce the synthesis error [26], [27], however it cannot be avoided. In this paper, we are only interested in issues on compression that causes distortion. We directly investigate the relationship between the quality of virtual view and  $Q$  of texture map ( $Q^T$ ) or depth map ( $Q^D$ ).

Since the virtual view is projected from pixel value in the texture map, its quality will be affected by the quality of decoded texture map. In Fig. 4, the quality influence of texture map on virtual view is investigated by changing  $Q^T$  from 2 to 30 meanwhile fixing  $Q^D$  at 14, 18 and 22 respectively. The quality of virtual view ( $P^s$ ) is measured in term of PSNR. As shown in Fig. 4, once  $Q^D$  is determined, the  $P^s$ - $Q^T$  relationship can be approximated as linear.

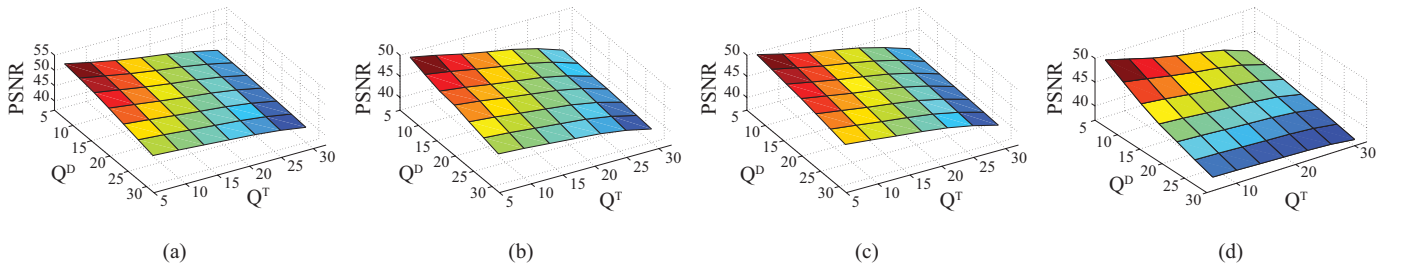


Fig. 6. Joint relationship between quality of synthesized view and  $Q^T$  and  $Q^D$ . (a) *Pantomime*. (b) *Balloons*. (c) *Kendo*. (d) *Champagne\_tower*.

Similarly in Fig. 5,  $Q^D$  is changed from 2 to 30, while  $Q^T$  is fixed at 14, 18, 22 respectively. We can see that linearity also can be observed between  $P^s$  and  $Q^D$ . Therefore we have the  $P^s$ - $Q^T$  relationship as

$$\frac{\partial P^s(Q^T, Q^D)}{\partial Q^T} = \beta(Q^D) \quad (8)$$

and the  $P^s$ - $Q^D$  relationship as

$$\frac{\partial P^s(Q^T, Q^D)}{\partial Q^D} = \gamma(Q^T). \quad (9)$$

Moreover, we can observe that the values of  $\beta(Q^D)$  or  $\gamma(Q^T)$  change slowly with  $Q^D$  or  $Q^T$ . Table I shows the slopes of linear  $P^s$ - $Q^T$  relation and linear  $P^s$ - $Q^D$  relation in Fig. 4 and Fig. 5, when the corresponding  $Q^D$  or  $Q^T$  are fixed at 14, 18, 22. In Table I, the derivatives of  $\beta(Q^D)$  and  $\gamma(Q^T)$  ( $\Delta\beta(Q^D)/\Delta Q^D$  and  $\Delta\gamma(Q^T)/\Delta Q^T$ ), which indicate the change rate with  $Q^D$  or  $Q^T$ , are very small. Therefore for simplicity, we approximate  $\beta(Q^D)$  and  $\gamma(Q^T)$  as constant and approximate (8) as

$$\frac{\partial P^s(Q^T, Q^D)}{\partial Q^T} = \beta \quad (10)$$

and (9) as

$$\frac{\partial P^s(Q^T, Q^D)}{\partial Q^D} = \gamma \quad (11)$$

where  $\beta$  and  $\gamma$  are considered as constants and their values depend on the video content.

In Fig. 6, the joint  $P^s$ - $Q^T$ - $Q^D$  relationship is illustrated by carrying out extensive experiments, where depth and texture maps are coded with  $Q$  from 6 to 30 respectively. The relation in Fig. 6 can be approximated as 2D plane which indicates linear and decoupled relation between the  $P^s$ - $Q^T$  and  $P^s$ - $Q^D$ . For the completely decoupled linear relations, ideally the derivatives of  $\beta(Q^D)$  and  $\gamma(Q^T)$  should be 0. As shown in Table I, the actual derivatives are very close to 0, which indicates the approximation is close to the ideal cases, thus the caused approximation error is neglected in the rest of the paper.

### III. RATE CONTROL SCHEME

#### A. RDO Bit Allocation at Sequence Level

The reference relation between the coded views and the virtual views is illustrated in Fig. 7, where V1, V3 and V5 are coded views, and V2 and V4 are virtual views synthesized with

TABLE I  
SLOPE OF  $P^s$ - $Q^T$  RELATION AND  $P^s$ - $Q^D$  RELATION

|                  |          | Q = 14  | Q = 18  | Q = 22  | Der    |
|------------------|----------|---------|---------|---------|--------|
| <i>Champagne</i> | $\gamma$ | -0.3076 | -0.2853 | -0.2636 | 0.0055 |
|                  | $\beta$  | -0.1214 | -0.1088 | -0.0942 | 0.0034 |
| <i>Kendo</i>     | $\gamma$ | -0.0835 | -0.0756 | -0.0694 | 0.0018 |
|                  | $\beta$  | -0.2789 | -0.2604 | -0.2557 | 0.0029 |
| <i>Pantomime</i> | $\gamma$ | -0.1215 | -0.1103 | -0.0977 | 0.0030 |
|                  | $\beta$  | -0.3056 | -0.2762 | -0.2533 | 0.0065 |
| <i>Balloons</i>  | $\gamma$ | -0.1293 | -0.1215 | -0.1095 | 0.0025 |
|                  | $\beta$  | -0.2319 | -0.2180 | -0.1847 | 0.0059 |

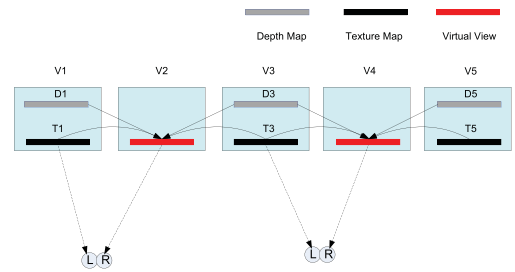


Fig. 7. Illustration of the reference relationship of the virtual view and the coded view.

the texture and depth maps of V1, V3 and V3, V5 respectively. Since both the coded views and virtual views will be presented for human, their qualities are equally important. Due to the limitation of the transmission capacity or the storage space, the problem is how to allocate bit reasonably to optimize the overall quality performance. For convenience, in the rest of this paper the superscripts  $T$  and  $D$  are used to indicate the texture map and depth map; the subscripts  $n$ ,  $m$  and  $i$ ,  $j$  stand for the view index. The optimization problem is formulated as

$$\text{Max} \left( \sum_{n \in C} P_n(Q_n^T) + \sum_{m \in S} P_m(\vec{Q}^T, \vec{Q}^D) \right) \quad (12)$$

where  $C$  is the set of the coded view index, e.g.  $C = \{1, 3, 5\}$ ;  $S$  is the set of virtual view index, e.g.  $S = \{2, 4\}$ ;  $P_n(Q_n^T)$  and  $P_m(\vec{Q}^T, \vec{Q}^D)$  are the quality of  $n$ th view and  $m$ th view. Since the quality of coded view is determined by the corresponding  $Q^T$ ,  $P_n$  is the function of  $Q_n^T$ . For virtual view, its quality is determined by both the  $Q^T$  and  $Q^D$  of the nearby coded views. For example,  $P_2$  is determined by  $Q_1^T, Q_3^T$  and  $Q_1^D, Q_3^D$  as illustrated in Fig. 7. In general,  $P_m$  is function of  $\vec{Q}^T$  and  $\vec{Q}^D$ , where  $\vec{Q}^T = [Q_1^T, Q_3^T, \dots]$  and  $\vec{Q}^D = [Q_1^D, Q_3^D, \dots]$ .

The optimization problem is under the constraint that

$$\sum_{n \in C} \left( R_n^D(Q_n^T) + R_n^D(Q_n^D) \right) < R_{tot} \quad (13)$$

where  $R_n^T$  and  $R_n^D$  are the bits to code the  $n$ th texture and depth map respectively;  $R_{tot}$  is total target bits. It is obvious that the optimization problem is generally convex, since  $P$  of the coded view and virtual view have linear relationship with  $Q^T$  and  $Q^D$  as discussed in section II. By applying the method of Lagrangian multiplier, we have

$$J = \left( \sum_{n \in C} P_n(Q_n^T) + \sum_{m \in S} P_m(\vec{Q}^T, \vec{Q}^D) \right) + \lambda \left( \sum_{n \in C} \left( R_n^T(Q_n^T) + R_n^D(Q_n^D) \right) - R_{tot} \right) \quad (14)$$

where  $\lambda$  is Lagrangian multiplier. The  $Q$  values of texture and depth map have different effects on the total quality.  $Q^D$  only affects the quality of virtual view while  $Q^T$  influences the quality of both coded views and virtual views. Therefore depending on the type of  $Q$  value (*i.e.*,  $Q^T$  or  $Q^D$ ), we have different differential equations for (14). According to (7) and (10), the partial derivative of the first term of right side of (14) with respect to  $Q^T$  is derived as

$$\frac{\partial \left( \sum_{n \in C} P_n + \sum_{m \in S} P_m \right)}{\partial Q_i^T} = \alpha_i + \sum_{j \in K_i} \beta_{ij} \quad (15)$$

where  $\alpha_i$  is the slope of linear  $P_i-Q_i^T$  relation in (7);  $\beta_{ij}$  is the slope of linear  $P_j-Q_i^T$  relation in (10);  $K_i$  is the set of virtual views whose qualities depend on  $i$ th coded view. For example in Fig. 7,  $K_1 = \{2\}$  since the 1st view only affects the 2nd virtual view, while  $K_3 = \{2, 4\}$  since the 3rd view affects the 2nd and 4th virtual views. Therefore  $Q^T$  in different positions have different effects on the total quality, and thus the right side of (15) varies for different views.

Meanwhile, by taking the partial derivative of the second term of right side of (14) with respect to  $Q^T$ , and combining with (4) we obtain

$$\frac{\partial R_i^T}{\partial Q_i^T} = \tau_i \cdot c_1 \cdot R_i^T \quad (16)$$

where  $R_i^T$  is bits for texture map. Finally, for the optimal solution, by differentiating (14) on both sides and replacing with (15) and (16), we get

$$0 = k_i^T + \lambda \cdot \tau_i^T \cdot c_1 \cdot R_i^{T*} \quad (17)$$

where  $R_i^{T*}$  is optimal bit for the texture map of  $i$ th view;  $k_i^T$  is a parameter of the texture map related to the view position that

$$k_i^T = \alpha_i + \sum_{j \in K_i} \beta_{ij}. \quad (18)$$

Similarly the partial derivative of the first term of right side of (14) with respect to  $Q_n^D$  is derived from (11) as

$$\frac{\partial \left( \sum_{n \in C} P_n + \sum_{m \in S} P_m \right)}{\partial Q_i^D} = \sum_{j \in K_i} \gamma_{ij} \quad (19)$$

where  $\gamma_{ij}$  is the slope of linear  $P_j-Q_i^D$  relation in (11). By taking the partial derivative of (14) with respect to  $Q_i^D$  and replacing with (19), we have

$$0 = k_i^D + \lambda \cdot \tau_i^D \cdot c_1 \cdot R_i^{D*} \quad (20)$$

where  $R_i^T$  is the optimal bits for  $i$ th texture map;  $k_i^D$  is model parameter of the depth map in  $i$ th view that

$$k_i^D = \sum_{j \in K_i} \gamma_{ij}. \quad (21)$$

Therefore from (17) and (20) we can get the optimal bit allocation for both depth or texture map of  $i$ th view as

$$R_i^* = \frac{k_i / \tau_i}{\sum_{n \in C} (k_n^T / \tau_n^T + k_n^D / \tau_n^D)} R_{tot} \quad (22)$$

where  $\tau_i$  and  $k_i$  can be the parameters for either texture map or depth map. Therefore the bit allocation scheme in (22) can be applied both for the texture and depth map. In this way, optimal bit allocation among different views and among the texture and depth map are automatically achieved.

### B. Model Parameter Estimation

In order to allocate bits according to (22), we have to access model parameter  $\alpha_i$ ,  $\beta_{ij}$ ,  $\gamma_{ij}$  and  $\tau_i$  before coding. Therefore the texture map is precoded at  $Q_A^T$  and  $Q_B^T$  and the depth map is precoded at  $Q_A^D$  and  $Q_B^D$ . Based on (7), (10) and (11), these parameters can be estimated as

$$\alpha_i = \frac{P_{iA} - P_{iB}}{Q_{iA}^T - Q_{iB}^T} \quad (23)$$

$$\beta_{ij} = \frac{\hat{P}_{jA} - \hat{P}_{jB}}{Q_{iA}^T - Q_{iB}^T} \quad (24)$$

$$\gamma_{ij} = \frac{\check{P}_{jA} - \check{P}_{jB}}{Q_{iA}^D - Q_{iB}^D} \quad (25)$$

where  $P_{iA}$  and  $P_{iB}$  are the PSNR of  $i$ th coded view precoded at  $Q_A^T$  and  $Q_B^T$  respectively;  $\hat{P}_{jA}$  and  $\hat{P}_{jB}$  are the PSNR of  $j$ th virtual view synthesized with the  $i$ th texture map precoded at  $Q_A^T$  and  $Q_B^T$  respectively;  $\check{P}_{jA}$  and  $\check{P}_{jB}$  are the PSNR of  $j$ th virtual view synthesized with the  $i$ th depth map precoded at  $Q_A^D$  and  $Q_B^D$  respectively.

In order to estimate these parameters, each view has to be precoded twice, which would involve heavy computation, especially when the view number is large. Usually the video contents of different views are highly similar. Thus we assume the R-D characteristics are similar in the same type of videos. To reduce the computational complexity, instead of precoding  $m$  views, only the texture and the depth map of the first view are precoded. Then the model parameters  $\alpha$ ,  $\beta$ ,  $\gamma$  are

TABLE II  
MODEL PARAMETER VALUE AND THE CORRESPONDING ESTIMATION

|          |                | Newspaper |        |            | Champagne_tower |        |            | Balloon |        |            | Mobile |        |            |
|----------|----------------|-----------|--------|------------|-----------------|--------|------------|---------|--------|------------|--------|--------|------------|
|          |                | Actual    | Est    | E(%)       | Actual          | Est.   | E(%)       | Actual  | Est.   | E(%)       | Actual | Est.   | E(%)       |
| $\alpha$ | $\alpha_2$     | -0.515    | -0.512 | 0.6        | -0.406          | -0.405 | 0.1        | -0.413  | -0.434 | 5.3        | -0.739 | -0.736 | 0.4        |
|          | $\alpha_3$     | -0.535    | -0.512 | 4.3        | -0.420          | -0.405 | 3.5        | -0.405  | -0.434 | 7.2        | -0.746 | -0.736 | 1.3        |
| $\beta$  | $\beta_{32}$   | -0.240    | -0.242 | 0.8        | -0.112          | -0.104 | 7.0        | -0.255  | -0.258 | 1.4        | -0.525 | -0.514 | 2.1        |
|          | $\beta_{34}$   | -0.250    | -0.242 | 3.4        | -0.098          | -0.104 | 6.3        | -0.252  | -0.258 | 2.6        | -0.519 | -0.514 | 1.0        |
|          | $\beta_{54}$   | -0.263    | -0.242 | 8.0        | -0.105          | -0.104 | 1.1        | -0.256  | -0.258 | 0.9        | -0.541 | -0.514 | 5.0        |
| $\gamma$ | $\gamma_{32}$  | -0.167    | -0.151 | 9.5        | -0.251          | -0.256 | 2.1        | -0.102  | -0.107 | 5.4        | -0.143 | -0.155 | 8.5        |
|          | $\gamma_{34}$  | -0.144    | -0.151 | 4.9        | -0.278          | -0.256 | 7.8        | -0.096  | -0.107 | 11.5       | -0.146 | -0.155 | 5.6        |
|          | $\gamma_{54}$  | -0.167    | -0.151 | 9.7        | -0.281          | -0.256 | 9.0        | -0.101  | -0.107 | 6.9        | -0.132 | -0.155 | 17.1       |
| $\tau^T$ | $\tau_2^T$     | -1.126    | -1.073 | 4.7        | -1.370          | -1.314 | 4.1        | -1.103  | -1.045 | 5.3        | -1.137 | -1.093 | 3.9        |
|          | $\tau_3^T$     | -1.164    | -1.073 | 7.8        | -1.396          | -1.314 | 5.9        | -1.113  | -1.045 | 6.2        | -1.187 | -1.093 | 7.9        |
|          | $\tau_3^D$     | -1.048    | -1.010 | 3.6        | -0.832          | -0.922 | 10.8       | -0.956  | -0.993 | 3.8        | -0.727 | -0.721 | 0.9        |
| $\rho$   | $\rho_2^T$     | 19435     | 21041  | 8.3        | 50493           | 48792  | 3.4        | 23864   | 23637  | 1.0        | 6438   | 6618   | 2.8        |
|          | $\rho_3^T$     | 22032     | 21991  | 0.2        | 60480           | 57388  | 5.1        | 25290   | 25786  | 2.0        | 8040   | 7596   | 5.5        |
|          | <b>Average</b> |           |        | <b>5.0</b> |                 |        | <b>4.9</b> |         |        | <b>4.5</b> |        |        | <b>5.5</b> |

TABLE III  
RESULT SUMMARY OF DIFFERENT RC ALGORITHMS ON THE SEQUENCE *Balloons*

| Target View (Mbps) | Liu2011     |      |            |       | Yuan2011    |            |             |            | Liu2009         |             |            |             | Proposed+CQ |                 |             |            | Proposed+FL |            |                 |             |
|--------------------|-------------|------|------------|-------|-------------|------------|-------------|------------|-----------------|-------------|------------|-------------|-------------|-----------------|-------------|------------|-------------|------------|-----------------|-------------|
|                    | Rate (kbps) |      | PSNR (dB)  | E (%) | Rate (kbps) |            | PSNR (dB)   | E (%)      | $\Delta P$ (dB) | Rate (kbps) |            | PSNR (dB)   | E (%)       | $\Delta P$ (dB) | Rate (kbps) |            | PSNR (dB)   | E (%)      | $\Delta P$ (dB) |             |
|                    | T           | D    |            | T     | D           |            |             |            | T               | D           |            |             |             | T               | D           |            |             |            |                 |             |
| 3 (Mbps)           | V1          | 832  | 211        | 41.13 | 718         | 265        | 41.31       |            |                 | 642         | 412        | 40.79       |             |                 | 725         | 129        | 41.36       |            |                 |             |
|                    | V2          |      |            | 40.71 |             |            | 41.09       |            |                 |             |            | 41.06       |             |                 |             |            | 40.96       |            |                 |             |
|                    | V3          | 811  | 203        | 41.05 | 692         | 244        | 41.24       | <b>2.0</b> | <b>0.29</b>     | 619         | 374        | 40.74       | <b>5.5</b>  | <b>-0.03</b>    | 1006        | 166        | 42.51       | <b>0.2</b> | <b>0.62</b>     |             |
|                    | V4          |      |            | 40.58 |             |            | 41.06       |            |                 |             |            | 41.02       |             |                 |             |            | 40.82       |            |                 |             |
|                    | V5          | 828  | 210        | 40.82 | 712         | 309        | 41.05       |            |                 | 635         | 484        | 40.54       |             |                 | 865         | 103        | 41.74       |            |                 |             |
| 4 (Mbps)           | V1          | 1126 | 281        | 42.27 | 908         | 353        | 42.30       |            |                 | 913         | 472        | 42.33       |             |                 | 1015        | 173        | 42.57       |            |                 |             |
|                    | V2          |      |            | 41.74 |             |            | 42.06       |            |                 |             |            | 42.34       |             |                 |             |            | 41.88       |            |                 |             |
|                    | V3          | 1106 | 269        | 42.12 | 880         | 321        | 42.19       | <b>5.6</b> | <b>0.16</b>     | 885         | 426        | 42.22       | <b>4.0</b>  | <b>0.29</b>     | 1311        | 232        | 43.33       | <b>0.7</b> | <b>0.48</b>     |             |
|                    | V4          |      |            | 41.62 |             |            | 42.00       |            |                 |             |            | 42.28       |             |                 |             |            | 41.72       |            |                 |             |
|                    | V5          | 1143 | 278        | 41.98 | 903         | 413        | 41.98       |            |                 | 909         | 557        | 42.02       |             |                 | 1149        | 148        | 42.63       |            |                 |             |
| 5 (Mbps)           | V1          | 1381 | 346        | 43.09 | 1164        | 450        | 43.09       |            |                 | 1059        | 708        | 42.81       |             |                 | 1178        | 226        | 43.16       |            |                 |             |
|                    | V2          |      |            | 42.49 |             |            | 42.81       |            |                 |             |            | 43.04       |             |                 |             |            | 42.56       |            |                 |             |
|                    | V3          | 1344 | 336        | 42.89 | 1136        | 406        | 42.93       | <b>2.9</b> | <b>0.18</b>     | 1029        | 633        | 42.67       | <b>6.7</b>  | <b>0.11</b>     | 1814        | 288        | 43.92       | <b>1.1</b> | <b>0.21</b>     |             |
|                    | V4          |      |            | 42.31 |             |            | 42.76       |            |                 |             |            | 42.95       |             |                 |             |            | 42.33       |            |                 |             |
|                    | V5          | 1371 | 349        | 42.62 | 1169        | 530        | 42.71       |            |                 | 1060        | 844        | 42.45       |             |                 | 1366        | 182        | 42.45       |            |                 |             |
| <b>Average:</b>    |             |      | <b>3.6</b> |       |             | <b>3.5</b> | <b>0.21</b> |            |                 |             | <b>5.4</b> | <b>0.12</b> |             |                 |             | <b>0.7</b> | <b>0.43</b> |            | <b>0.4</b>      | <b>0.25</b> |

TABLE IV  
RESULT SUMMARY OF DIFFERENT RC ALGORITHMS ON THE SEQUENCE *Newspaper*

| Target View (Mbps) | Liu2011     |      |            |       | Yuan2011    |            |              |            | Liu2009         |             |            |             | Proposed+CQ |                 |             |            | Proposed+FL |            |                 |             |
|--------------------|-------------|------|------------|-------|-------------|------------|--------------|------------|-----------------|-------------|------------|-------------|-------------|-----------------|-------------|------------|-------------|------------|-----------------|-------------|
|                    | Rate (kbps) |      | PSNR (dB)  | E (%) | Rate (kbps) |            | PSNR (dB)    | E (%)      | $\Delta P$ (dB) | Rate (kbps) |            | PSNR (dB)   | E (%)       | $\Delta P$ (dB) | Rate (kbps) |            | PSNR (dB)   | E (%)      | $\Delta P$ (dB) |             |
|                    | T           | D    |            | T     | D           |            |              |            | T               | D           |            |             |             | T               | D           |            |             |            |                 |             |
| 3 (Mbps)           | V2          | 885  | 227        | 39.96 | 577         | 377        | 39.31        |            |                 | 670         | 329        | 39.93       |             |                 | 720         | 215        | 40.22       |            |                 |             |
|                    | V3          |      |            | 37.64 |             |            | 37.92        |            |                 |             |            | 38.11       |             |                 |             |            | 38.12       |            |                 |             |
|                    | V4          | 798  | 209        | 39.56 | 540         | 400        | 38.95        | <b>6.7</b> | <b>-0.22</b>    | 634         | 347        | 39.57       | <b>2.1</b>  | <b>0.26</b>     | 831         | 342        | 40.59       | <b>2.3</b> | <b>0.50</b>     |             |
|                    | V5          |      |            | 38.46 |             |            | 38.67        |            |                 |             |            | 38.99       |             |                 |             |            | 38.96       |            |                 |             |
|                    | V6          | 722  | 191        | 38.96 | 550         | 354        | 38.64        |            |                 | 648         | 310        | 39.29       |             |                 | 623         | 201        | 39.16       |            |                 |             |
| 4 (Mbps)           | V2          | 1152 | 304        | 40.90 | 741         | 538        | 40.37        |            |                 | 748         | 569        | 40.42       |             |                 | 963         | 309        | 41.30       |            |                 |             |
|                    | V3          |      |            | 38.30 |             |            | 38.95        |            |                 |             |            | 39.00       |             |                 |             |            | 38.92       |            |                 |             |
|                    | V4          | 1088 | 279        | 40.54 | 702         | 575        | 40.00        | <b>5.7</b> | <b>-0.02</b>    | 710         | 610        | 40.06       | <b>2.7</b>  | <b>0.04</b>     | 1094        | 488        | 41.57       | <b>0.7</b> | <b>0.61</b>     |             |
|                    | V5          |      |            | 39.26 |             |            | 39.78        |            |                 |             |            | 39.88       |             |                 |             |            | 39.95       |            |                 |             |
|                    | V6          | 987  | 253        | 39.94 | 722         | 495        | 39.74        |            |                 | 730         | 523        | 39.79       |             |                 | 846         | 270        | 40.28       |            |                 |             |
| 5 (Mbps)           | V2          | 1498 | 373        | 41.75 | 970         | 631        | 41.34        |            |                 | 882         | 830        | 41.04       |             |                 | 1134        | 375        | 41.94       |            |                 |             |
|                    | V3          |      |            | 38.82 |             |            | 39.61        |            |                 |             |            | 39.92       |             |                 |             |            | 39.51       |            |                 |             |
|                    | V4          | 1347 | 347        | 41.32 | 932         | 680        | 40.98        | <b>4.8</b> | <b>0.19</b>     | 844         | 905        | 40.67       | <b>1.8</b>  | <b>0.08</b>     | 1487        | 599        | 42.47       | <b>0.8</b> | <b>0.69</b>     |             |
|                    | V5          |      |            | 39.89 |             |            | 40.64        |            |                 |             |            | 40.69       |             |                 |             |            | 40.71       |            |                 |             |
|                    | V6          | 1208 | 313        | 40.58 | 968         | 579        | 40.73        |            |                 | 875         | 757        | 40.42       |             |                 | 1099        | 345        | 41.18       |            |                 |             |
| <b>Average</b>     |             |      | <b>1.4</b> |       |             | <b>5.7</b> | <b>-0.02</b> |            |                 |             | <b>2.2</b> | <b>0.13</b> |             |                 |             | <b>1.3</b> | <b>0.60</b> |            | <b>0.5</b>      | <b>0.46</b> |

calculated according to (23), (24), (25) and they are used to predict the other similar parameters as

$$\alpha_i = \alpha, \quad \beta_{ij} = \beta, \quad \gamma_{ij} = \gamma \quad (26)$$

Meanwhile from (4), we can estimate  $\tau_i$  for the texture map or the depth map as

$$\tau_i = \frac{\ln(R_{iA}) - \ln(R_{iB})}{\ln(Q_{SiA}) - \ln(Q_{SiB})} \quad (27)$$

TABLE V  
 RESULT SUMMARY OF DIFFERENT RC ALGORITHMS ON THE SEQUENCE *Champagne\_Tower*

| Target View<br>(Mbps) | Liu2011 |      |      |        | Yuan2011 |      |       |        | Liu2009    |       |       |        | Proposed+CQ |            |      |        | Proposed+FL |     |            |        |      |       |      |            |
|-----------------------|---------|------|------|--------|----------|------|-------|--------|------------|-------|-------|--------|-------------|------------|------|--------|-------------|-----|------------|--------|------|-------|------|------------|
|                       | Rate    |      | PSNR | E      | Rate     |      | PSNR  | E      | $\Delta P$ | Rate  |       | PSNR   | E           | $\Delta P$ | Rate |        | PSNR        | E   | $\Delta P$ | Rate   |      | PSNR  | E    | $\Delta P$ |
|                       | (kbps)  | (dB) | (%)  | (kbps) | (dB)     | (%)  | (dB)  | (kbps) | (dB)       | (%)   | (dB)  | (kbps) | (dB)        | (%)        | (dB) | (kbps) | (dB)        | (%) | (dB)       | (kbps) | (dB) | (%)   | (dB) |            |
| 3<br>(Mbps)           | V38     | 891  | 240  | 41.48  | 567      | 603  | 40.29 | 521    | 720        | 39.96 | 628   | 331    | 40.78       | 617        | 292  | 40.60  |             |     |            |        |      |       |      |            |
|                       | V39     |      |      | 39.05  |          |      | 40.35 |        |            | 39.79 |       |        | 39.90       |            |      | 39.47  |             |     |            |        |      |       |      |            |
|                       | V40     | 640  | 171  | 41.20  | 518      | 471  | 40.39 | 5.6    | -0.12      | 474   | 388   | 40.05  | 2.8         | -0.55      | 761  | 479    | 41.92       | 5.4 | 0.33       | 769    | 410  | 41.82 | 3.9  | 0.13       |
|                       | V41     |      |      | 38.60  |          |      | 39.82 |        |            | 39.31 |       |        | 39.87       |            |      | 39.44  |             |     |            |        |      |       |      |            |
|                       | V42     | 823  | 217  | 40.99  | 544      | 464  | 39.85 | 525    | 455        | 39.48 | 645   | 318    | 40.48       | 620        | 410  | 40.66  |             |     |            |        |      |       |      |            |
| 4<br>(Mbps)           | V38     | 1239 | 315  | 42.27  | 713      | 1035 | 41.22 | 646    | 1051       | 40.93 | 819   | 433    | 41.67       | 823        | 390  | 41.68  |             |     |            |        |      |       |      |            |
|                       | V39     |      |      | 39.59  |          |      | 41.38 |        |            | 41.11 |       |        | 40.84       |            |      | 40.46  |             |     |            |        |      |       |      |            |
|                       | V40     | 896  | 233  | 41.83  | 649      | 571  | 41.37 | 7.4    | 0.31       | 590   | 534   | 41.09  | 3.2         | 0.00       | 1003 | 630    | 42.69       | 4.5 | 0.69       | 1020   | 545  | 42.73 | 0.1  | 0.52       |
|                       | V41     |      |      | 39.12  |          |      | 41.04 |        |            | 40.54 |       |        | 41.08       |            |      | 40.53  |             |     |            |        |      |       |      |            |
|                       | V42     | 1121 | 285  | 41.47  | 731      | 595  | 40.84 | 658    | 647        | 40.58 | 856   | 438    | 41.43       | 837        | 389  | 41.49  |             |     |            |        |      |       |      |            |
| 5<br>(Mbps)           | V38     | 1494 | 397  | 42.98  | 832      | 1292 | 41.77 | 852    | 1182       | 41.89 | 936   | 547    | 42.16       | 1035       | 487  | 42.33  |             |     |            |        |      |       |      |            |
|                       | V39     |      |      | 40.10  |          |      | 42.13 |        |            | 41.83 |       |        | 41.44       |            |      | 41.14  |             |     |            |        |      |       |      |            |
|                       | V40     | 1107 | 292  | 42.52  | 759      | 636  | 41.93 | 3.3    | 0.35       | 777   | 590   | 42.06  | 0.1         | 0.31       | 1178 | 707    | 43.13       | 1.7 | 0.61       | 1303   | 681  | 43.30 | 2.4  | 0.50       |
|                       | V41     |      |      | 39.56  |          |      | 41.84 |        |            | 41.55 |       |        | 41.73       |            |      | 41.06  |             |     |            |        |      |       |      |            |
|                       | V42     | 1383 | 356  | 42.21  | 862      | 784  | 41.46 | 884    | 721        | 41.61 | 992   | 557    | 41.97       | 1033       | 583  | 42.03  |             |     |            |        |      |       |      |            |
| Average               |         |      | 1.1  |        |          | 5.4  | 0.18  |        |            | 2.0   | -0.08 |        |             | 3.8        | 0.54 |        |             |     |            | 2.1    | 0.38 |       |      |            |

where  $R_{iA}$  and  $R_{iB}$  refer to the output bits of texture map or depth map that are precoded at the corresponding  $Q_{s_{iA}}$  ( $Q_{iA}$ ) and  $Q_{s_{iB}}$  ( $Q_{iB}$ ).  $\tau^T$  of the texture and  $\tau^D$  of the depth map in the first view are used as estimation for those of other coded views.

On the other hand, the sequence complexity related parameter  $\rho_i$  needs to be estimated for the texture and depth map of each view. For the first view,  $\rho_1$  can be estimated according to precoding result as

$$\rho_1 = \frac{R_{1A} - R_{1B}}{e^{\tau_1(c_1 Q_{1A} + c_2)} - e^{\tau_1(c_1 Q_{1A} + c_2)}} \quad (28)$$

where  $\rho_1$  refers to model parameters for either the texture map or the depth map. Since  $R_A$  and  $R_B$  of other views are unavailable, a limited number of frames are encoded for the texture and depth map of each view, and the output bit rate is recorded as sample complexity  $r_i$ .  $\rho_i$  of other views is estimated as

$$\rho_i = \frac{r_i}{r_1} \rho_1 \quad (29)$$

In this way, we can estimate the model parameters with reduced computational complexity.

### C. Frame Level Bit Regulation

Given the total bit rate constraint, the optimal target bit rate ( $R_i^*$ ) for each texture or depth map of each view can be calculated according to (22). To achieve the target bit of the each sequence, two RC schemes can be applied. One is to apply RC at frame level (FL) to adjust  $Q$  dynamically along the sequence to achieve the target bit rate. The other is to adopt a constant  $Q$  (CQ) to code the entire sequence. Since the fluctuation in  $Q$  usually degrade the R-D performance, the CQ usually has better R-D performance than FL. On the other hand, FL has more accurate target bit rate achievement due to the adaptive adjustment of  $Q$  value.

In this paper, we adopt both the FL and the CQ schemes to achieve the target bit. For the FL scheme, bit allocation

algorithm in [28] is used to allocate target bit ( $R_i$ ) at frame level and the corresponding  $Q_s$  for the coding frame is calculated based on (2) as

$$Q_s = \left( \frac{R_i}{\rho} \right)^{1/\tau} \quad (30)$$

Then the corresponding  $Q$  can be attained with the  $Q$ - $Q_s$  relation.

For the CQ, with the target bit of the sequence, the  $Q$  can be calculated based on (4) as

$$Q = \frac{\ln(R^*/\rho) - c_2\tau}{c_1\tau} \quad (31)$$

where  $R^*$  is the target bit;  $\rho$  and  $\tau$  are the estimated model parameters. Since we have already accessed the R-D characteristics of the sequence and estimated these model parameters, the calculated  $Q$  lead to the achievement of the target bit.

## IV. EXPERIMENTAL RESULTS

The experiments are conducted under 5-view scenario as shown in Fig. 1, where 3 views are coded, and 2 virtual views are synthesized. The testing sequences include *Champagne\_tower* (1280×960), *Balloons* (1024×768) provided by Nagoya University [29], and *Newspaper* (1024×768) provided by Gwangju Institute of Science and Technology (GIST) [30]. The texture and depth map of three views are separately encoded with MVC encoder [31] as I-view, P-view and P-view respectively. For P-view, the interview prediction is only applied for key frames. View Synthesis Reference Software (VSRS) [32] is used to synthesize the virtual view. 201 frames are encoded for each view.

### A. Verification of Parameter Estimation Scheme

In this section, we verify the effectiveness of the proposed parameter estimation scheme in Section III-B. In the experiments,  $\alpha$ ,  $\beta$ ,  $\gamma$  are estimated according to (26), and  $\rho$  is

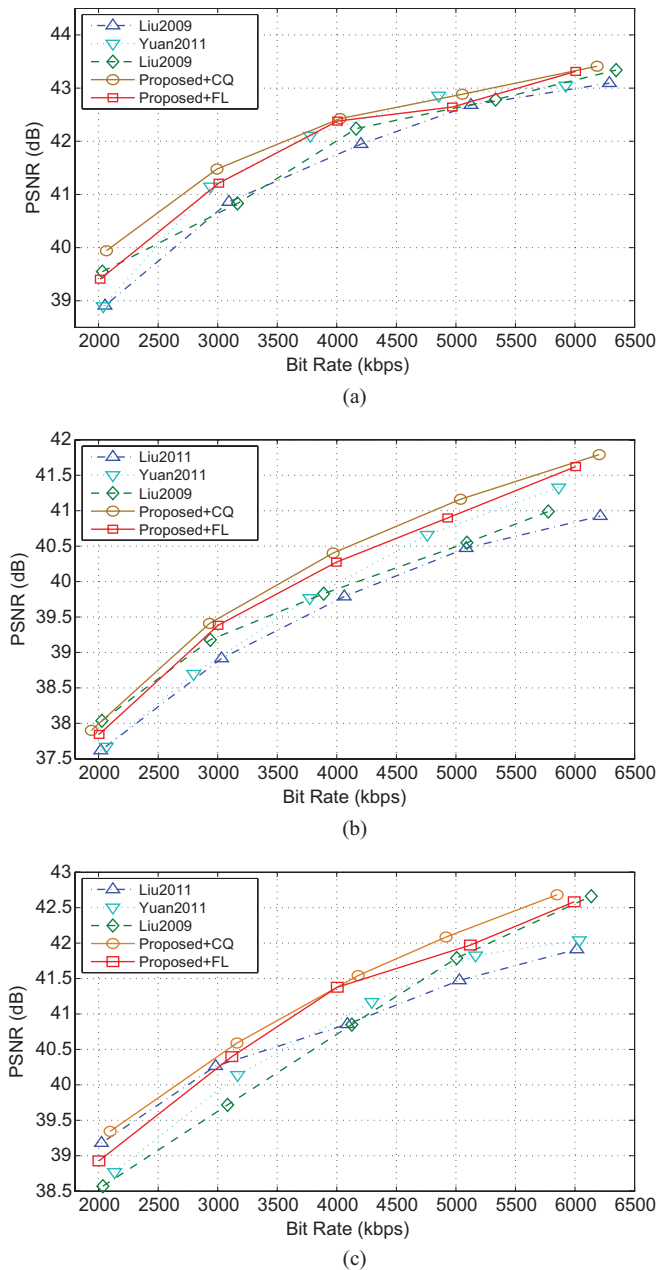


Fig. 8. R-D curves. The autostereoscopic 3-D video is set to 5-view scenario, where 3 views are coded views and 2 views are virtual views. The three-coded views are coded with MVC codec as I-view, P-view, and P-view, respectively. Search range is set to 96 with GOP size 4. Target bits are set at 2.0, 3.0, 4.0, 5.0, and 6.0 Mb/s and the corresponding R-D points are depicted for each algorithm. (a) *Balloons*. (b) *Newspaper*. (c) *Champagne\_tower*.

estimated according to (29), and  $\tau^T$  and  $\tau^D$  are estimated based on (27).

The results and the estimation errors are presented in Table II. We can see that the estimation is accurate enough that the mismatch is less than 5.5% on average, which indicates the proposed scheme can achieve accurate model parameter estimation.

### B. R-D Performance and Rate Accuracy

In order to evaluate the performance of the proposed RC algorithm, Liu2011 [15], Yuan2011 [14] and Liu2009 [13] are utilized for comparison. For the proposed algorithm, both the

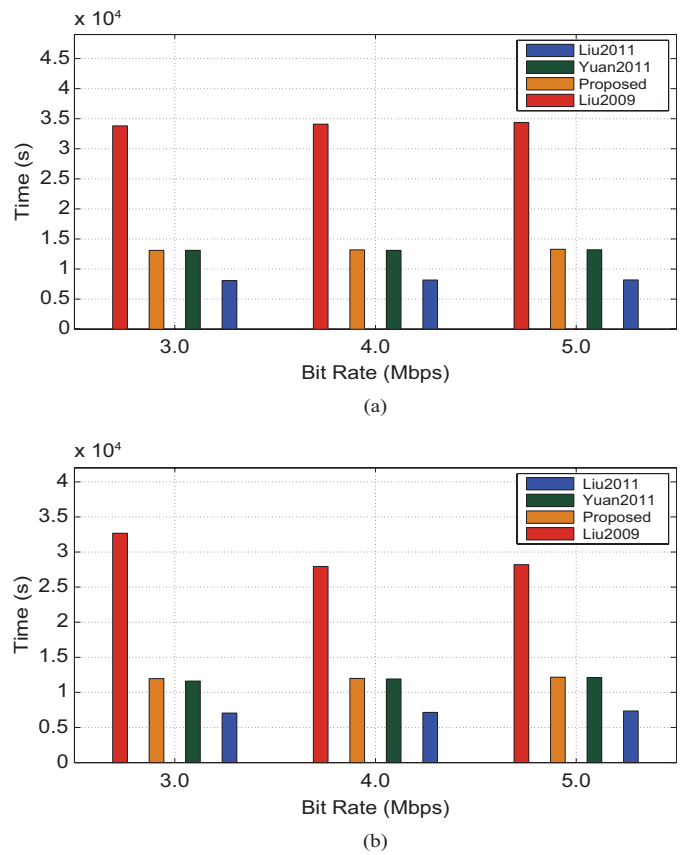


Fig. 9. Consumed coding time. The autostereoscopic 3-D video is set to 5-view scenario, where 3 views are coded views and 2 views are virtual views. The three-coded views are coded with MVC codec as I-view, P-view, and P-view, respectively. Search range is set to 96 with GOP size 4. Target bits are set at 3.0, 4.0, and 5.0 Mb/s for each algorithm. (a) *Balloons*. (b) *Newspaper*.

FL (proposed+FL) and the CQ (proposed+CQ) are employed to achieve the target bit for each sequence. Table III, IV and V summarize the output bits of the coded texture and the depth map of each view. Since the virtual views are generated with DIBR, for V2 and V4 in Table III and V3 and V5 in Table IV, V38 and V40 in Table V, there are no output bits for the texture and depth map. The ratio of output bits of the texture and depth map is fixed close to 4:1 for Liu2011.

To evaluate the accuracy of the bit rate achievement, the following measurement is adopted

$$E = \frac{|R_{all} - R_{target}|}{R_{target}} \times 100\% \quad (32)$$

where  $R_{all}$  is the total bits used to encode the depth map and texture map of three views;  $R_{target}$  is the target bit rate. Table III, IV and V present the rate achievement accuracy of different algorithms. We can see the proposed+FL generally has the best performance that its mismatch is 0.4%, 0.5%, 2.1% on average for different sequences. The proposed+CQ also achieves acceptable accuracy, i.e. 0.7%, 1.3% and 3.8% on average.

The PSNR of both coded and virtual views are recorded for each view. The average PSNR is used to evaluate the overall quality performance of five views for different algorithms. The average PSNR of Liu2011 is set as the benchmark and the



performances of other algorithms are measured as

$$\Delta P = P_i - \hat{P} \quad (33)$$

where  $\hat{P}$  refers to the average PSNR of Liu2011 and  $P_i$  refers to the average PSNR of the rest algorithms. The results are presented in Table III, IV, and V, where we can see the proposed+CQ achieves the best performance that the average PSNR gains are 0.43 dB, 0.60 dB and 0.54 respectively, while the proposed+FL has little degradation in R-D performance achieving 0.25 dB, 0.46 dB and 0.38 dB gain respectively.

For further illustration, typical R-D curves for different algorithms are shown in Fig. 8, where we can see the proposed+CQ demonstrates the best R-D efficiency among the different algorithms.

The computational complexity is compared for different algorithms. The computation complexity mainly comes from view coding and view synthesis process. For Liu2011, each view including the texture and depth map is coded with single pass, while for the proposed algorithm and Yuan2011, two additional iterations are required for the first view. For Liu2009, the texture maps of each view have to be coded for  $M$  times and the depth maps have to be code for three times, where  $M$  is the number of proper  $Q$  values which generate bit rate falling into the range  $[1/2R_t, R_t]$ . As for view synthesis, Liu2011 has to synthesize two virtual views, while for the proposed method and Yuan2011 three more virtual views need to be synthesized to assist model parameter calculation. For the Liu2009,  $3M$  more virtual view synthesis are required to calculate the model parameters. Therefore, Liu2011 consumes the lowest computation complexity. Although the proposed algorithm requires additional computation in the precoding stage, with the increase of view number, the portion of the additional complexity in the total complexity will decrease. The actual consuming time for each algorithm is presented in Fig. 9, where we can see the proposed algorithm takes less time than Liu2009 and is comparable with Yuan2011.

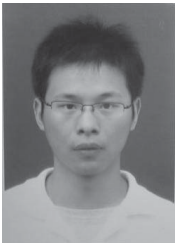
## V. CONCLUSION

In this paper, we proposed a RC scheme to achieve the best overall quality for 3DV. Based on power models for the  $R-Q_s$  and the  $MSE-Q_s$  relationship, we derived the exponential  $R-Q$  relationship and the linear  $PSNR-Q$  relationship. Furthermore, a linear model is approximated for the quality dependency between the virtual view and the coded view. Based on the above R-D characteristics of both the coded view and the virtual view, a R-D optimized RC algorithm is derived. Experiments are conducted on different video sequences and the results demonstrate the effectiveness of the proposed algorithm.

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